

Preparing for post-quantum and hybrid cryptography on the Internet

Douglas Stebila  McMaster
University

Funding acknowledgements:

Motivation

QCS 2017

Workshop on Quantum CyberSecurity

22 – 23 June, 2017, Canterbury, UK

Home

Program

Registration

Venue

Organising Committee



Banner photography © Mark Wheadon

Program

Thursday 22 June

09:00 – 10:00 Registration, Tea and Coffee



Secure Connection
The connection is secure.
www.cs.kent.ac.uk

Hide details

First Visited: No previous visits recorded
Certificate: www.cs.kent.ac.uk (Quovadis Limited)
Connection: TLS 1.0 AES_128_CBC HMAC-SHA1 RSA

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Banner photography © Mark Wheadon

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Secure Connection

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Certificate: www.cs.kent.ac.uk (QuoVadis Limited)

Connection: TLS 1.0 AES_128_CBC HMAC-SHA1 RSA

QuoVadis Root CA 2

QuoVadis Global SSL ICA G2

www.cs.kent.ac.uk



www.cs.kent.ac.uk

Issued by: QuoVadis Global SSL ICA G2

Expires: Friday, May 18, 2018 at 5:00:36 PM British Summer Time

✔ This certificate is valid

Details

OK

017
urity
UK

Registrati



Banner photography © Mark Wheadon

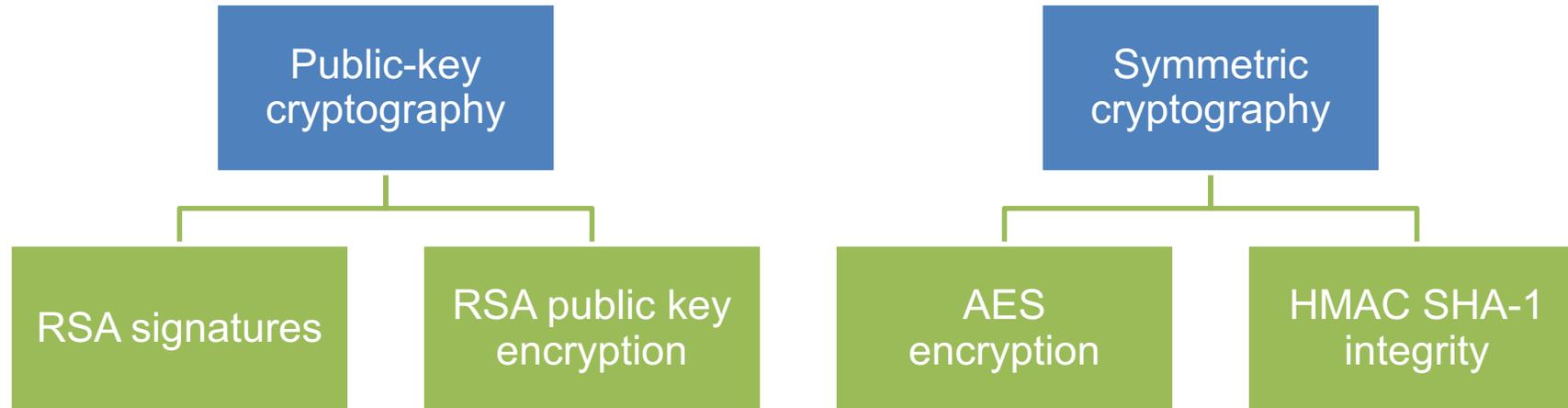
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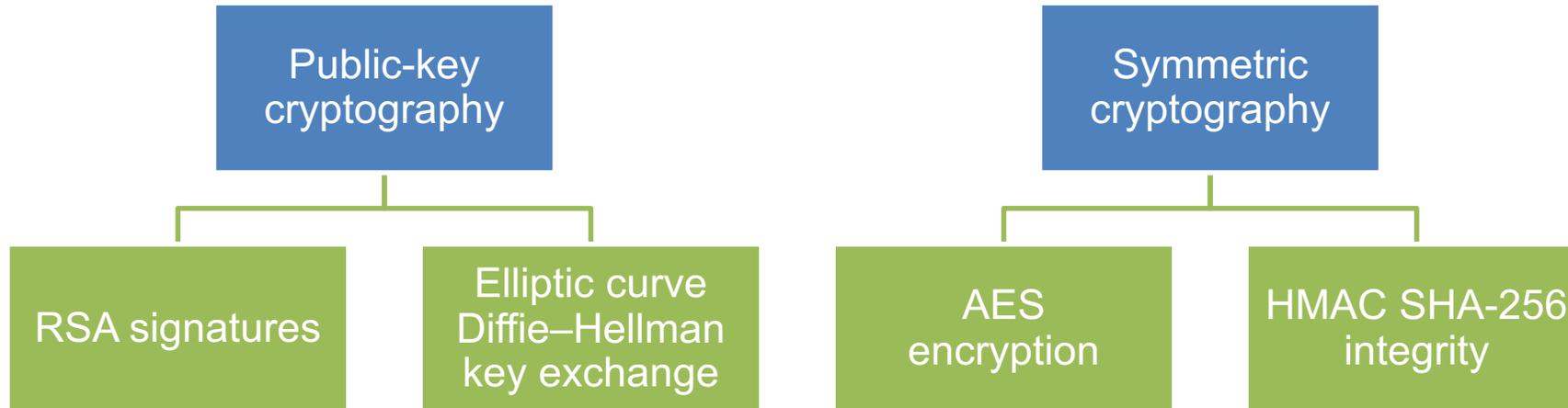
Contemporary cryptography

TLS 1.0 AES_128_CBC HMAC-SHA1 RSA

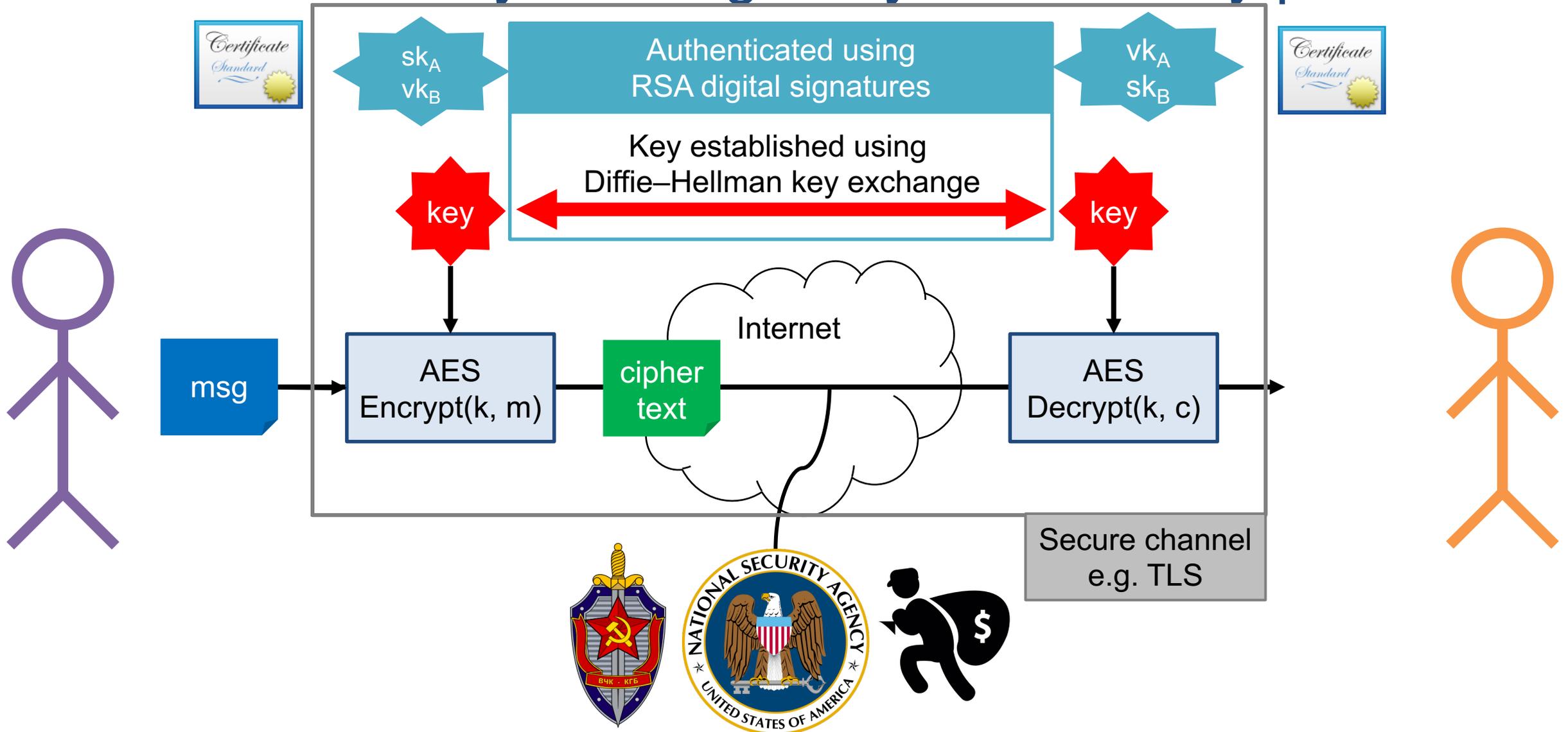


Contemporary cryptography

TLS 1.2 AES_128_GCM HMAC-SHA256 RSA + ECDH

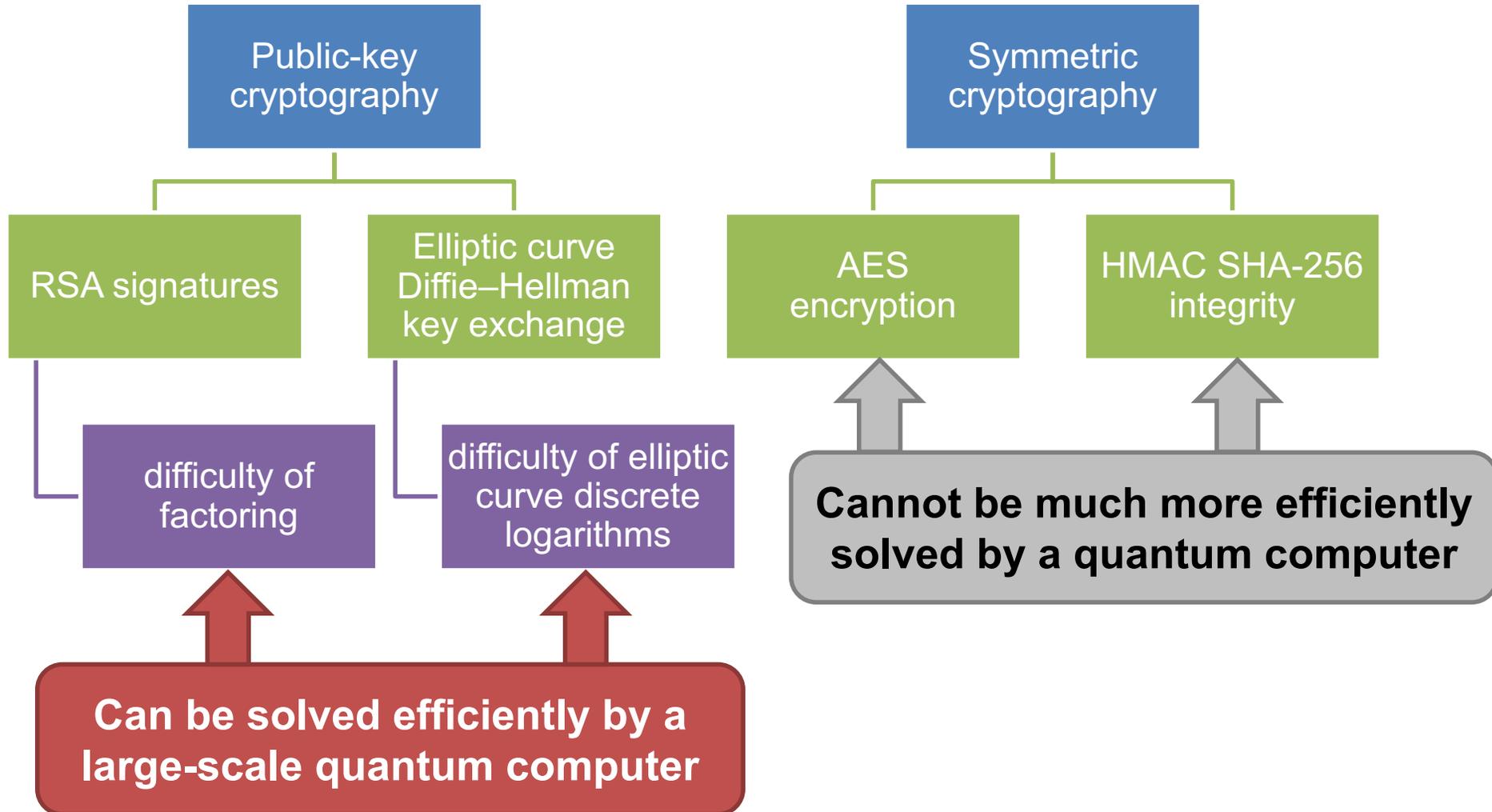


Authenticated key exchange + symmetric encryption

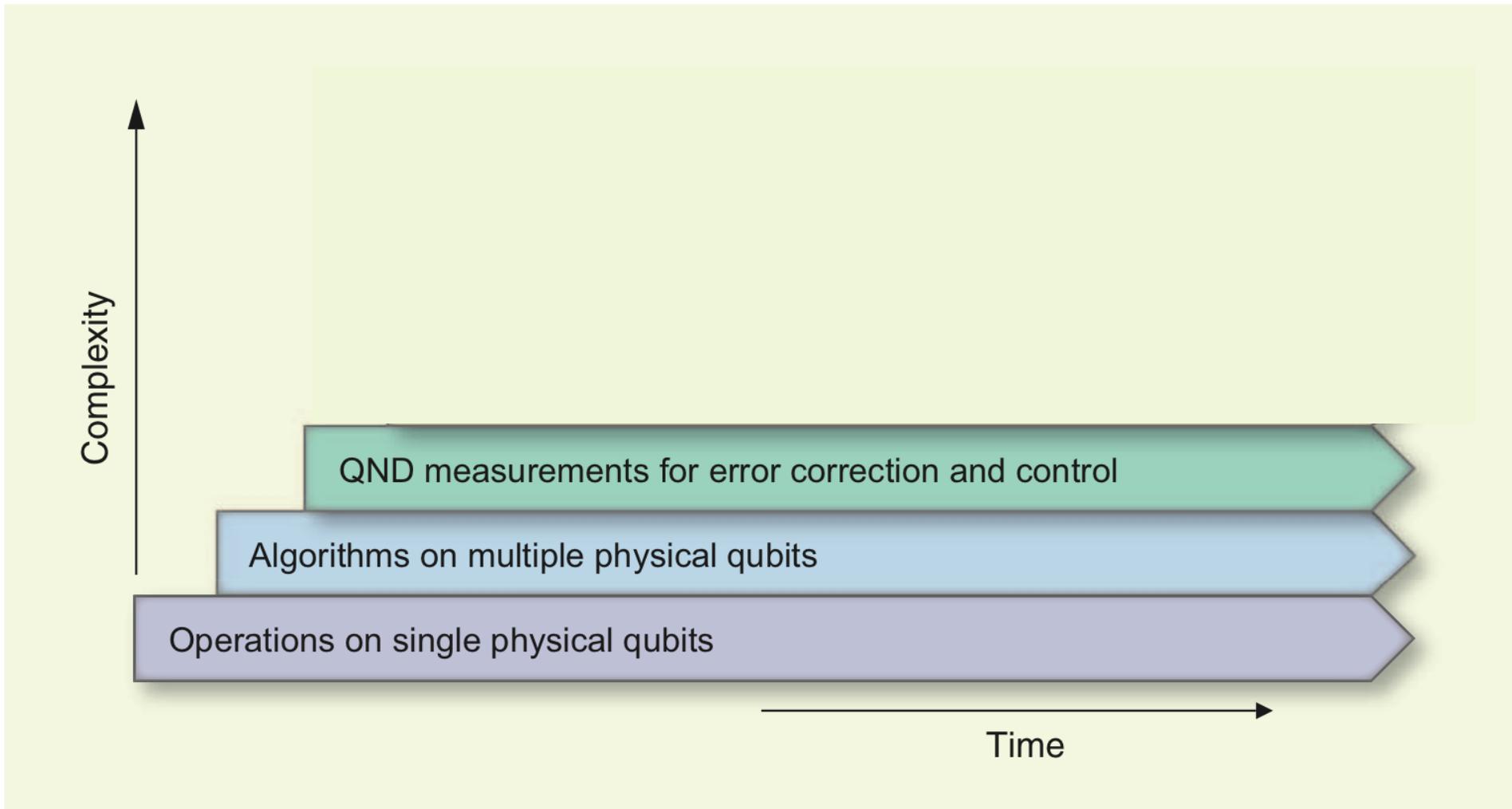


Contemporary cryptography

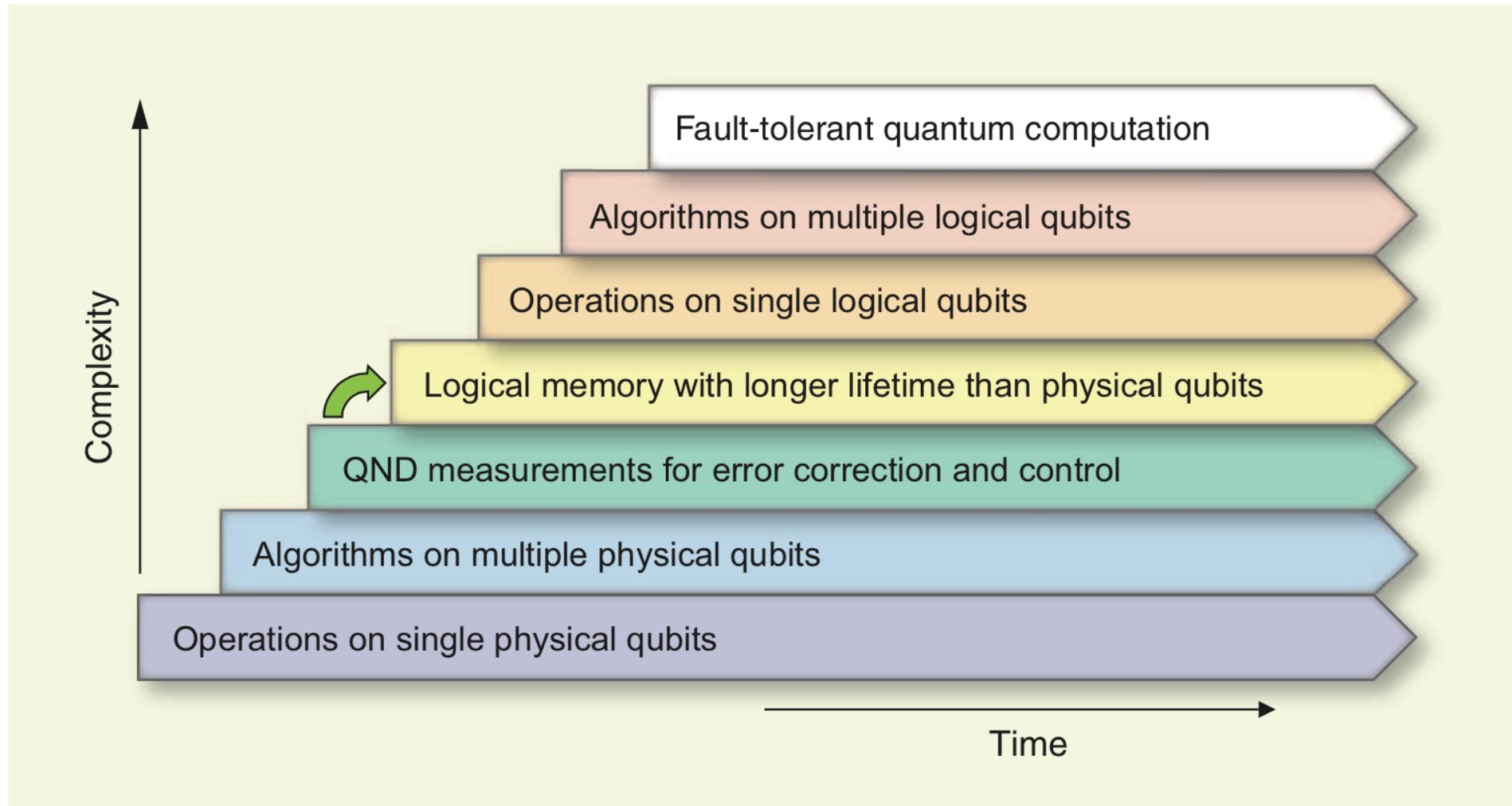
TLS 1.2 AES_128_GCM HMAC-SHA256 RSA + ECDH



When will a large-scale quantum computer be built?



When will a large-scale quantum computer be built?



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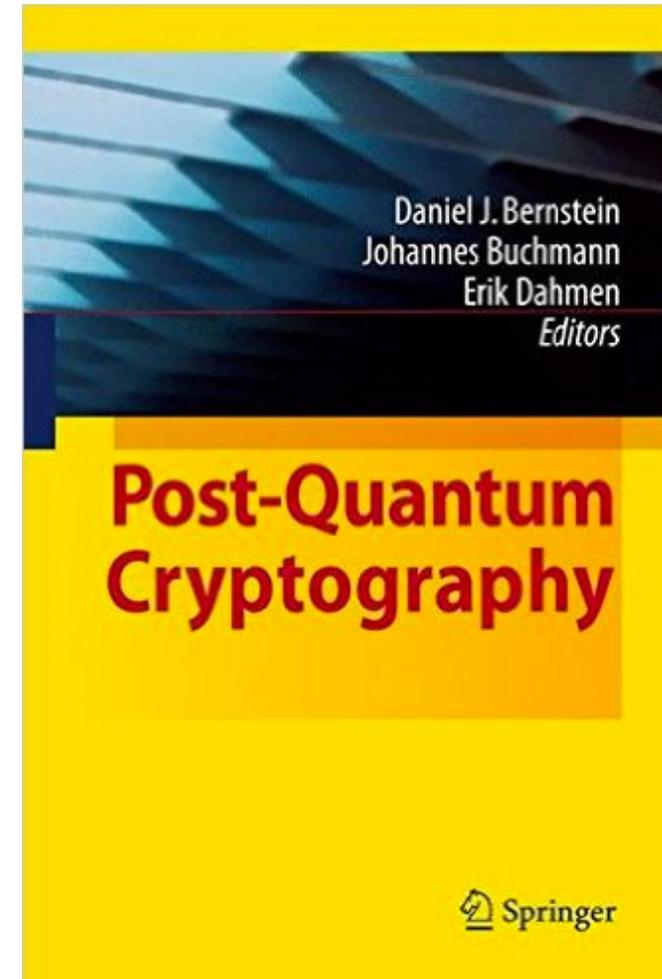
“I estimate a 1/7 chance of breaking RSA-2048 by 2026 and a 1/2 chance by 2031.”

— Michele Mosca, November 2015
<https://eprint.iacr.org/2015/1075>

Post-quantum cryptography in academia

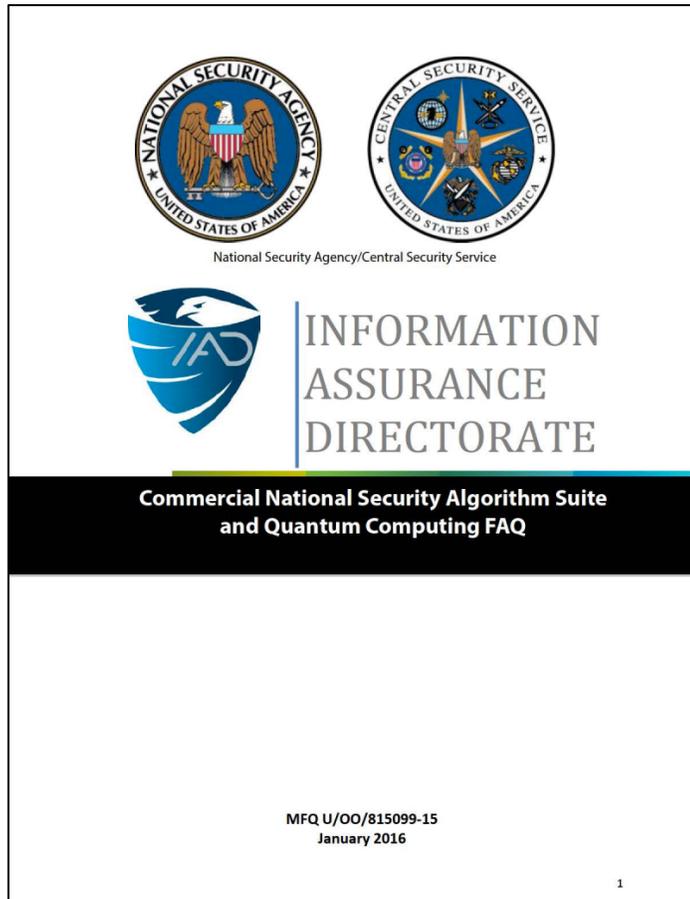
Conference series

- PQCrypto 2006
- PQCrypto 2008
- PQCrypto 2010
- PQCrypto 2011
- PQCrypto 2013
- PQCrypto 2014
- PQCrypto 2016
- PQCrypto 2017



2009

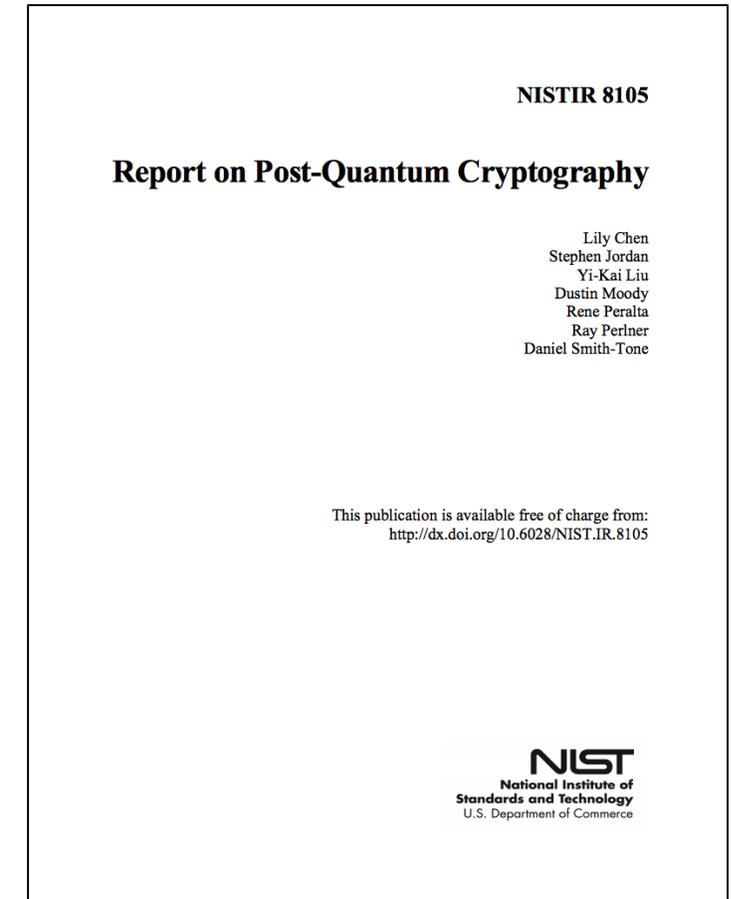
Post-quantum cryptography in government



Aug. 2015 (Jan. 2016)

“IAD will initiate a transition to quantum resistant algorithms in the not too distant future.”

– NSA Information Assurance Directorate,
Aug. 2015



Apr. 2016

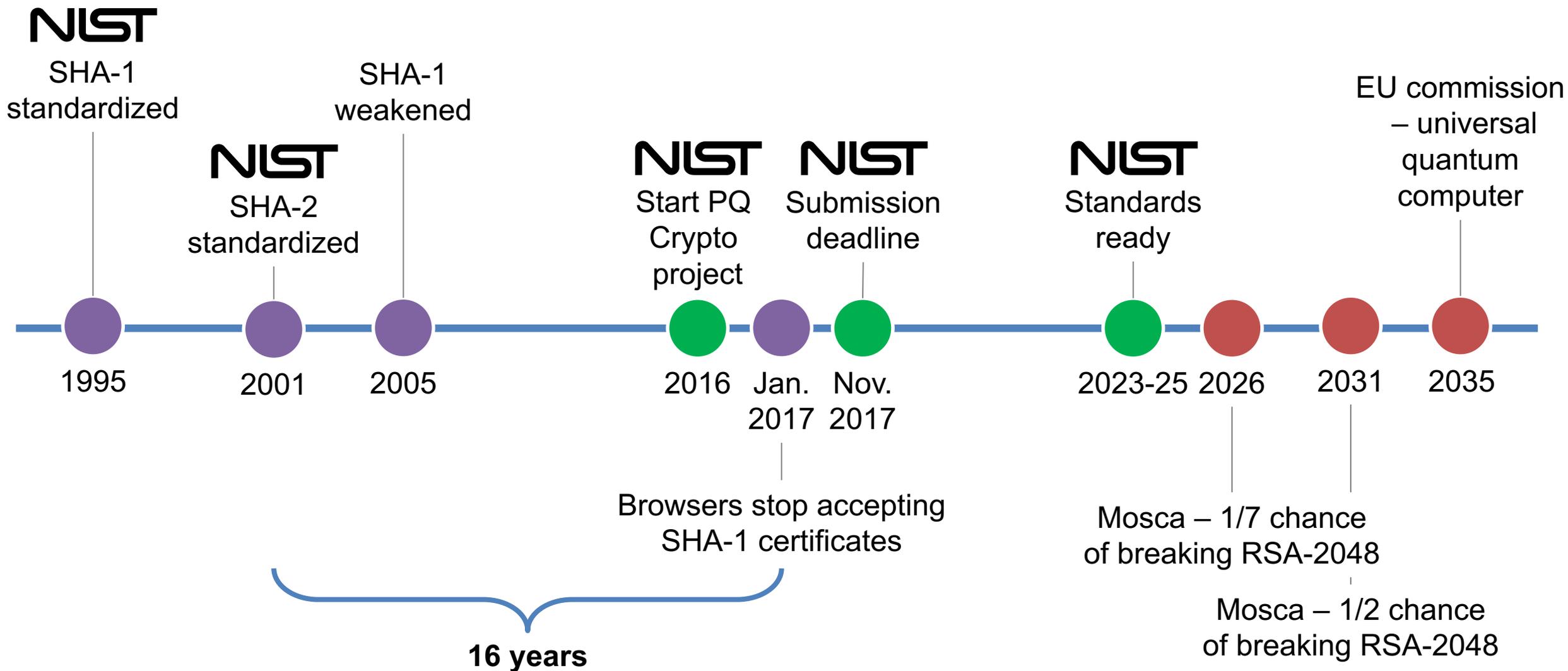
NIST Post-quantum Crypto Project timeline

<http://www.nist.gov/pqcrypto>

December 2016	Formal call for proposals
November 2017	Deadline for submissions
3-5 years	Analysis phase
2 years later (2023-2025)	Draft standards ready

"Our intention is to select a couple of options for more immediate standardization, as well as to eliminate some submissions as unsuitable. ... The goal of the process is **not primarily to pick a winner**, but to document the strengths and weaknesses of the different options, and to analyze the possible tradeoffs among them."

Timeline



Post-quantum crypto

Post-quantum crypto

Classical crypto with no known exponential quantum speedup

Hash-based

- Merkle signatures
- Sphincs

Code-based

- McEliece

Multivariate

- multivariate quadratic

Lattice-based

- NTRU
- learning with errors
- ring-LWE

Isogenies

- supersingular elliptic curve isogenies

Quantum-safe crypto

Classical post-quantum crypto

Hash-based

- Merkle signatures
- Sphincs

Code-based

- McEliece

Multivariate

- multivariate quadratic

Lattice-based

- NTRU
- learning with errors
- ring-LWE

Isogenies

- supersingular elliptic curve isogenies

Quantum crypto

Quantum key distribution

Quantum channels

Quantum blind computation

Post-quantum crypto research agenda

- Design better post-quantum schemes
- Improve classical and quantum attacks
- Pick parameter sizes
- Develop fast, secure implementations
- Integrate them into the existing infrastructure

This talk

- Frodo
 - Key exchange protocol from the learning with errors problem
- Open Quantum Safe project
 - A library for comparing post-quantum primitives
 - Framework for easing integration into applications like OpenSSL
- Hybrid key exchange and digital signatures
 - In TLS
 - In X.509v3, S/MIME

Learning with errors problems

Solving systems of linear equations

$$\begin{array}{c} \mathbb{Z}_{13}^{7 \times 4} \\ \begin{array}{|c|c|c|c|} \hline 4 & 1 & 11 & 10 \\ \hline 5 & 5 & 9 & 5 \\ \hline 3 & 9 & 0 & 10 \\ \hline 1 & 3 & 3 & 2 \\ \hline 12 & 7 & 3 & 4 \\ \hline 6 & 5 & 11 & 4 \\ \hline 3 & 3 & 5 & 0 \\ \hline \end{array} \end{array} \quad \times \quad \begin{array}{c} \text{secret} \\ \mathbb{Z}_{13}^{4 \times 1} \\ \begin{array}{|c|} \hline \\ \hline \\ \hline \\ \hline \\ \hline \end{array} \end{array} \quad = \quad \begin{array}{c} \mathbb{Z}_{13}^{7 \times 1} \\ \begin{array}{|c|} \hline 4 \\ \hline 8 \\ \hline 1 \\ \hline 10 \\ \hline 4 \\ \hline 12 \\ \hline 9 \\ \hline \end{array} \end{array}$$

Linear system problem: given **blue**, find **red**

Solving systems of linear equations

$$\mathbb{Z}_{13}^{7 \times 4} \quad \text{secret } \mathbb{Z}_{13}^{4 \times 1} \quad \mathbb{Z}_{13}^{7 \times 1}$$

4	1	11	10
5	5	9	5
3	9	0	10
1	3	3	2
12	7	3	4
6	5	11	4
3	3	5	0

 \times

6
9
11
11

 $=$

4
8
1
10
4
12
9

Easily solved using
Gaussian elimination
(Linear Algebra 101)

Linear system problem: given **blue**, find **red**

Learning with errors problem

random $\mathbb{Z}_{13}^{7 \times 4}$ secret $\mathbb{Z}_{13}^{4 \times 1}$ small noise $\mathbb{Z}_{13}^{7 \times 1}$ $\mathbb{Z}_{13}^{7 \times 1}$

4	1	11	10
5	5	9	5
3	9	0	10
1	3	3	2
12	7	3	4
6	5	11	4
3	3	5	0

×

6
9
11
11

+

0
-1
1
1
1
0
-1

=

4
7
2
11
5
12
8

Learning with errors problem

random $\mathbb{Z}_{13}^{7 \times 4}$

4	1	11	10
5	5	9	5
3	9	0	10
1	3	3	2
12	7	3	4
6	5	11	4
3	3	5	0

secret $\mathbb{Z}_{13}^{4 \times 1}$

×

+

small noise $\mathbb{Z}_{13}^{7 \times 1}$

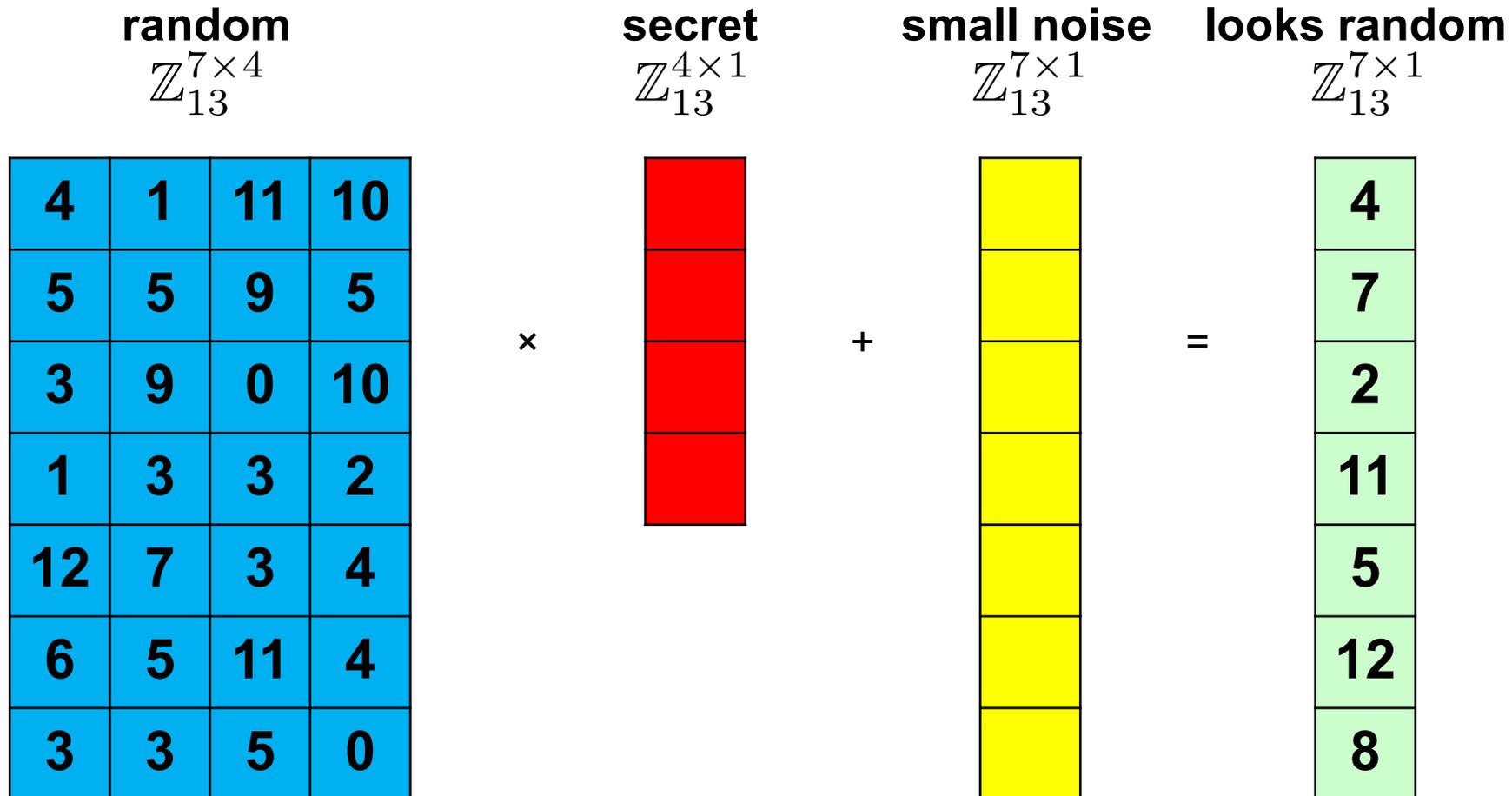
=

$\mathbb{Z}_{13}^{7 \times 1}$

4
7
2
11
5
12
8

Computational LWE problem: given blue, find red

Decision learning with errors problem



Decision LWE problem: given **blue**, distinguish **green** from random

Ring learning with errors problem

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
10	4	1	11
11	10	4	1
1	11	10	4
4	1	11	10
10	4	1	11
11	10	4	1

Each row is the cyclic shift of the row above

Ring learning with errors problem

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
3	4	1	11
2	3	4	1
12	2	3	4
9	12	2	3
10	9	12	2
11	10	9	12

Each row is the cyclic shift of the row above

...

with a special wrapping rule:
 x wraps to $-x \pmod{13}$.

Ring learning with errors problem

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
---	---	----	----

Each row is the cyclic shift of the row above

...

with a special wrapping rule:
 x wraps to $-x \pmod{13}$.

So I only need to tell you the first row.

Ring learning with errors problem

$$\mathbb{Z}_{13}[x]/\langle x^4 + 1 \rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

×

$$6 + 9x + 11x^2 + 11x^3$$

secret

+

$$0 - 1x + 1x^2 + 1x^3$$

small noise

=

$$10 + 5x + 10x^2 + 7x^3$$

Ring learning with errors problem

$$\mathbb{Z}_{13}[x]/\langle x^4 + 1 \rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

×



secret

+



small noise

=

$$10 + 5x + 10x^2 + 7x^3$$

Computational ring-LWE problem: given blue, find red

Problems

Computational
LWE problem

Decision
LWE problem

with or without
short secrets

Computational
ring-LWE problem

Decision
ring-LWE problem

Hardness of decision LWE

worst-case gap shortest
vector problem (GapSVP)

poly-time [Regev05, BLPRS13]

decision LWE

tight [ACPS09]

decision LWE
with short secrets

Practice:

- Assume the best way to solve DLWE is to solve LWE.
- Assume solving LWE involves a lattice reduction problem.
- Estimate parameters based on runtime of lattice reduction algorithms.
- (Ignore non-tightness.)

Key agreement from LWE

Bos, Costello, Ducas, Mironov, Naehrig, Nikolaenko, Raghunathan, Stebila.
Frodo: Take off the ring! Practical, quantum-safe key exchange from LWE.
ACM Conference on Computer and Communications Security (CCS) 2016.

<https://eprint.iacr.org/2016/659>

Basic LWE-DH key agreement (unauthenticated)

Based on Lindner–Peikert LWE public key encryption scheme

public: “big” A in $\mathbf{Z}_q^{n \times m}$

Alice

secret:

random “small” s, e in \mathbf{Z}_q^m

$$b = As + e$$

Bob

secret:

random “small” s', e' in \mathbf{Z}_q^n

$$b' = s'A + e'$$

shared secret:

$$b's = s'As + e's \approx s'As$$

shared secret:

$$s'b \approx s'As$$

These are only approximately equal \Rightarrow need rounding

Parameters

“Recommended”

- 144-bit classical security,
130-bit quantum security,
103-bit plausible lower bound
- $n = 752, m = 8, q = 2^{15}$
- χ = approximation to rounded
Gaussian with 11 elements
- Failure: $2^{-38.9}$
- Total communication: 22.6 KiB

“Paranoid”

- 177-bit classical security,
161-bit quantum security,
128-bit plausible lower bound
- $n = 864, m = 8, q = 2^{15}$
- χ = approximation to rounded
Gaussian with 13 elements
- Failure: $2^{-33.8}$
- Total communication: 25.9 KiB

LWE and ring-LWE public key encryption and key exchange

Regev

STOC 2005

- Public key encryption from LWE

Lyubashevsky, Peikert, Regev

Eurocrypt 2010

- Public key encryption from ring-LWE

Lindner, Peikert

ePrint 2010, CT-RSA 2011

- Public key encryption from LWE and ring-LWE
- Approximate key exchange from LWE

Ding, Xie, Lin

ePrint 2012

- Key exchange from LWE and ring-LWE with single-bit reconciliation

Peikert

PQCrypto 2014

- Key encapsulation mechanism based on ring-LWE and variant single-bit reconciliation

Bos, Costello, Naehrig, Stebila

IEEE S&P 2015

- Implementation of Peikert's ring-LWE key exchange, testing in TLS 1.2

“NewHope”

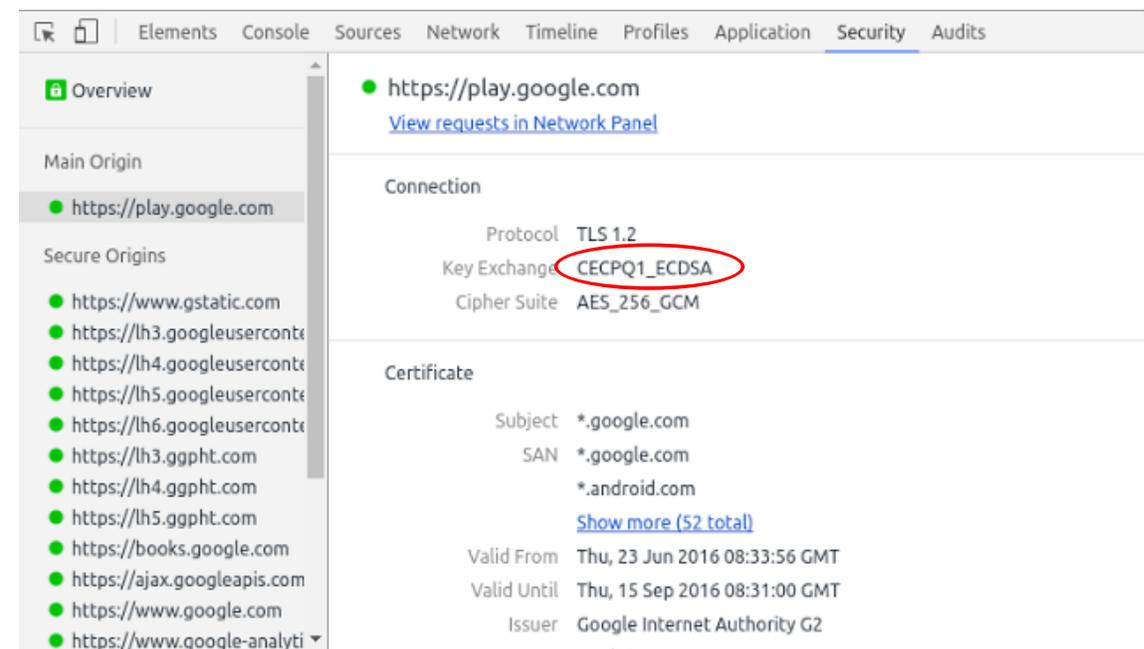
Alkim, Ducas, Pöppelman, Schwabe.
USENIX Security 2016

- New parameters
- Different error distribution
- Improved performance
- Pseudorandomly generated parameters
- Further performance improvements by others [GS16, LN16, AOPPS17, ...]

Google Security Blog

Experimenting with Post-Quantum Cryptography

July 7, 2016



The screenshot shows the Chrome DevTools Security panel for the URL <https://play.google.com>. The panel is divided into two main sections: Connection and Certificate. The Connection section shows the following details:

Property	Value
Protocol	TLS 1.2
Key Exchange	CECPQ1_ECDSA
Cipher Suite	AES_256_GCM

The Certificate section shows the following details:

Property	Value
Subject	*.google.com
SAN	*.google.com *.android.com
Valid From	Thu, 23 Jun 2016 08:33:56 GMT
Valid Until	Thu, 15 Sep 2016 08:31:00 GMT
Issuer	Google Internet Authority G2

The Key Exchange field, CECPQ1_ECDSA, is circled in red in the original image.

Why consider (slower, bigger) LWE?

Generic vs. ideal lattices

- Ring-LWE matrices have additional structure
 - Relies on hardness of a problem in **ideal** lattices
- LWE matrices have no additional structure
 - Relies on hardness of a problem in **generic** lattices
- NTRU also relies on a problem in a type of ideal lattices
- Currently, best algorithms for ideal lattice problems are essentially the same as for generic lattices
 - Small constant factor improvement in some cases
 - Very recent quantum polynomial time algorithm for Ideal-SVP (<http://eprint.iacr.org/2016/885>) but not immediately applicable to ring-LWE

If we want to eliminate this additional structure, can we still get an efficient protocol?

Implementations

Our implementations

- Ring-LWE BCNS15
- LWE Frodo

Pure C implementations

Constant time

Compare with others

- RSA 3072-bit (OpenSSL 1.0.1f)
- ECDH nistp256 (OpenSSL)

Use assembly code

- Ring-LWE NewHope
- NTRU EES743EP1
- SIDH (Isogenies) (MSR)

Pure C implementations

Post-quantum key exchange performance

	Speed		Communication	
RSA 3072-bit	Fast	4 ms	Small	0.3 KiB
ECDH <code>nistp256</code>	Very fast	0.7 ms	Very small	0.03 KiB
Code-based	Very fast	0.5 ms	Very large	360 KiB
NTRU	Very fast	0.3–1.2 ms	Medium	1 KiB
Ring-LWE	Very fast	0.2–1.5 ms	Medium	2–4 KiB
LWE	Fast	1.4 ms	Large	11 KiB
SIDH	Slow	35–400 ms	Small	0.5 KiB

Post-quantum signature sizes

	Public key		Signature	
RSA 3072-bit	Small	0.3 KiB	Small	0.3 KiB
ECDSA <i>nistp256</i>	Very small	0.03 KiB	Very small	0.03 KiB
Hash-based (stateful)	Small	0.9 KiB	Medium	3.6 KiB
Hash-based (stateless)	Small	1 KiB	Large	32 KiB
Lattice-based (ignoring tightness)	Medium	1.5–8 KiB	Medium	3–9 KiB
Lattice-based (respecting tightness)	Very large	1330 KiB	Small	1.2 KiB
SIDH	Small	1.5 KiB	Very large	704 KiB

Open Quantum Safe

<https://openquantumsafe.org/>

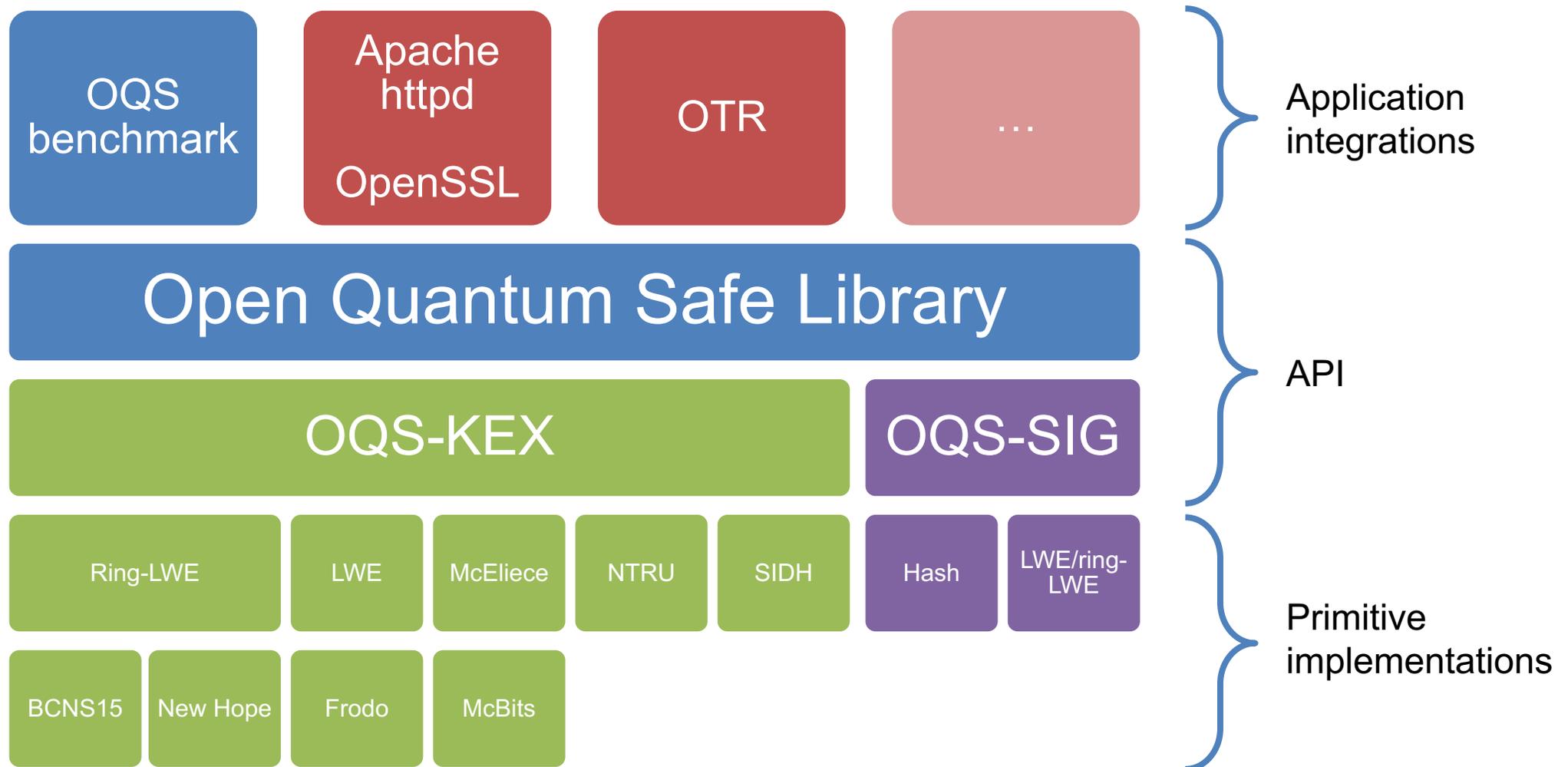
Open Quantum Safe

- MIT-licensed open-source project on Github
 - <https://openquantumsafe.org/>
 - <https://github.com/open-quantum-safe/>
- liboqs: C language library, common API

Open Quantum Safe

1. Collect post-quantum implementations together
 - Our own software
 - Thin wrappers around existing open source implementations
 - Contributions from others
2. Enable direct comparison of implementations
3. Support prototype integration into application level protocols
 - Don't need to re-do integration for each new primitive – how we did Frodo experiments

Open Quantum Safe architecture



liboqs: Current key exchange algorithms

- **Ring-LWE:**
 - BCNS15
 - NewHope
 - MSR NewHope improvements
- **LWE:** Frodo
- **NTRU**
- **SIDH (Supersingular isogeny Diffie–Hellman):**
 - MSR
 - IQC
- **Code:** McBits

liboqs: Benchmarking

- Built-in key exchange benchmarking suite
 - `./test_kex --bench`
- Gives cycle counts and ms runtimes

liboqs: Application integrations

OpenSSL v1.0.2:

- Ciphersuites using key exchange algorithms from liboqs
- Integrated into `openssl speed` benchmarking command and `s_client` and `s_server` command-line programs
- Track OpenSSL 1.0.2 stable with regular updates
 - <https://github.com/open-quantum-safe/openssl>
- Successfully used in Apache httpd and OpenVPN (with no modifications!)

OQC contributors and acknowledgements

Project leaders

- Michele Mosca and Douglas Stebila

Planning & discussions

- Scott Vanstone and Sherry Shannon Vanstone (Trustpoint)
- Matthew Campagna (Amazon Web Services)
- Alfred Menezes, Ian Goldberg, and Guang Gong (University of Waterloo)
- William Whyte and Zhenfei Zhang (Security Innovation)
- Jennifer Fernick, David Jao, and John Schanck (University of Waterloo)

Software contributors

- Mike Bender
- Tancrède Lepoint (SRI)
- Shравan Mishra (IQC)
- Christian Paquin (MSR)
- Alex Parent (IQC)
- Douglas Stebila (McMaster)
- Sebastian Verschoor (IQC)

+ Existing open-source code

Getting involved and using OQS

<https://openquantumsafe.org/>

If you're writing post-quantum implementations:

- We'd love to coordinate on API
- And include your software if you agree

If you want to prototype or evaluate post-quantum algorithms in applications:

- Maybe OQS will be helpful to you

We'd love help with:

- Code review and static analysis
- Signature scheme implementations
- Additional application-level integrations

Hybrid cryptography

Hybrid TLS: joint work with John Schanck

Hybrid signatures: joint work with Nina Bindel, Udyani Herath, Matthew McKague

Retroactive decryption

- A passive adversary that records today's communication can decrypt once they get a quantum computer
 - Not a problem for some people
 - Is a problem for other people
- How to provide potential post-quantum security to early adopters?

Hybrid ciphersuites

- Use pre-quantum and post-quantum algorithms together
- Secure if either one remains unbroken

Need to consider backward compatibility for non-hybrid-aware systems

Why hybrid?

- Potential post-quantum security for early adopters
- Maintain compliance with older standards (e.g. FIPS)
- Reduce risk from uncertainty on PQ assumptions/parameters

Hybrid ciphersuites

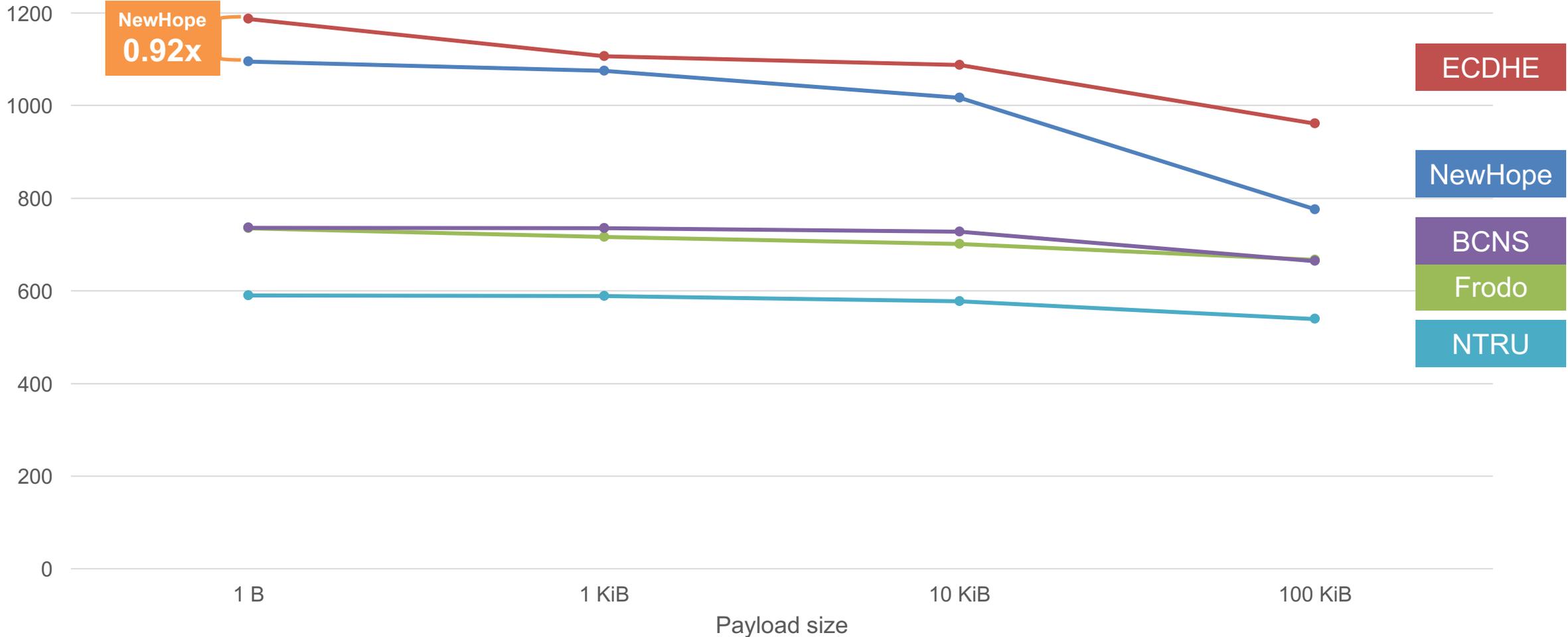
	Key exchange	Digital signature
1	Hybrid traditional + PQ	Single traditional
2	Hybrid traditional + PQ	Hybrid traditional + PQ
3	Single PQ	Single traditional
4	Single PQ	Single PQ

Likely focus
for next 10 years

TLS connection throughput – hybrid w/ECDHE

ECDSA signatures

bigger (top) is better



Compatibility of large extensions in certs in TLS

	Extension size in KiB				
	1.5	3.5	9.0	43.0	1333.0
<i>Libraries</i> (library's command-line client talking to library's command-line server)					
GnuTLS 3.5.11	✓	✓	✓	✓	×
Java SE 1.8.0_131	✓	✓	✓	✓	✓
mbedTLS 2.4.2	✓	✓	✓	×	×
NSS 3.29.1	✓	✓	✓	✓	×
OpenSSL 1.0.2k	✓	✓	✓	✓	×
<i>Web browsers</i> (talking to OpenSSL's command-line server)					
Apple Safari 10.1 (12603.1.30.0.34)	✓	✓	✓	✓	✓
Google Chrome 58.0.3029.81	✓	✓	✓	✓	×
Microsoft Edge 38.14393.1066.0	✓	✓	✓	×	×
Microsoft IE 11.1066.14393.0	✓	✓	✓	×	×
Mozilla Firefox 53.0	✓	✓	✓	✓	×
Opera 44.0.2510.1218	✓	✓	✓	✓	×

Summary

Preparing for post-quantum and hybrid cryptography on the Internet

Douglas Stebila



- **Learning with Errors (LWE)** can achieve reasonable key sizes and runtime with more conservative assumption
- **Open Quantum Safe** project allows for prototyping and comparison on post-quantum algorithms
- **Hybrid cryptography** will probably play a role in the transition

LWE key exchange (Frodo)

- <https://github.com/lwe-frodo>
- <https://eprint.iacr.org/2016/659>

Open Quantum Safe

- <https://openquantumsafe.org/>
- <https://eprint.iacr.org/2016/1017>

Hybrid PKI

- <https://eprint.iacr.org/2017/460>